Table 8- Differences between the computed and original coordinates of check points

| N o. of check points | X difference $(\mathrm{m})$ | Y difference $(\mathrm{m})$ | Z difference $(\mathrm{m})$ |
| :--- | :--- | :--- | :--- |
| 1 | -129.731752 | -11.974557 | 160.179949 |
| 2 | 72.548069 | -49.088296 | -27.601637 |
| 3 | -82.080482 | -11.393840 | 328.139363 |
| 4 | 11.532023 | 11.374207 | 28.591644 |
| 5 | 101.427132 | 31.563932 | -97.454667 |
| 6 | 27.624292 | -34.065214 | 66.129042 |
| 7 | 124.570777 | -17.617602 | -143.900027 |
| 8 | 19.254656 | -28.832136 | -40.352941 |

Table 9-RMSE of check points obtained by DLT (method 2)

| M ethod | X \& Y RM SE of check points $(\mathrm{m})$ | Z RM SE of check points $(\mathrm{m})$ |
| :--- | :--- | :--- |
| DLT | 124.311 | 10.418 |
|  | X \& Y RM SE of control points $(\mathrm{m})$ | Z RMSE of control points $(\mathrm{m})$ |
| DLT | 49.091 | 10.379 |

Table 10- Differences between the computed and original coordinates of check points

| No. of check points | X difference $(m)$ | Y difference $(m)$ | Z difference $(m)$ |
| :--- | :--- | :--- | :--- |
| 1 | -83.400867 | -8.514500 | -8.587859 |
| 2 | 35.946747 | -84.456549 | -5.897525 |

Table 11- The results of the proposed R adargrammetry algorithm converted to UTM projection system

| Point <br> Types | Points | X Diff. (m) | Y Diff. (m) | Height Diff. <br> $(\mathrm{m})$ | RM SE of X \& Y <br> $(\mathrm{m})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Control <br> Points | \#1 (flat) | 11.805000000051 | 34.933999999892 | 6.20172825 | 36.874684825686 |
|  | $\# 2$ (flat) | 15.253000000026 | 11.571999999695 | -0.3204760 | 19.145892326912 |
|  | $\# 3$ (flat) | 57.553000000 | 181.9879999998 | 34.917059 | 190.87163213262 |
|  | $\# 4$ (flat) | 41.386999999988 | 129.8030000 | 24.945258 | 136.24133946082 |
|  | $\# 1$ (flat) | 104.88599999994 | -98.46999999 | 11.182440 | 143.86595808576 |
|  | $\# 2$ (flat) | 111.88000 | -249.570999999 | -64.936943 | 273.50103919546 |
|  | $\# 3$ (mount.) | 28.233000000 | -529.4859999995 | -70.5161502 | 530.2381790144 |
|  | $\# 4$ (mount.) | -807.0990000 | 269.419000000 | 282.8959206 | 850.87918846461 |
|  | $\# 5$ (mount.) | -702.35700 | 217.20699999 | 327.9989647 | 735.1763300719 |
|  | $\# 6$ (mount.) | -34.6169999 | -628.39399999 | -103.013437 | 629.34676921774 |

## References

Crosetto, M. \& A rgues Pereze F., 1999-Radargrammetry and SAR interferometry for DEM generation: validation and data fusion. Proceedings of a Conference held 26-29 October, Toulouse, France. European SpaceA gency, 2000. E SA -SP vol. 450, ISBN: 9290926414, p. 367.
Liu, H., Zhao Z. \& Jezek, K. C., 2004 - Correction of positional errors and geometric distortions in topographic maps and DEM s using rigorous SAR simulation technique, Photogrammetric Engineering \& Remote Sensing, Vol. 70, No. 9, 1031-1042
Leberl, F. W., 1990 - R adargrammetric Image Processing. A rtech House.

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Table 3- Point wise polynomial results

| N umber of nearest points | RM SE of check points using <br> moving average | RM SE of check points using <br> weighted distance |
| :--- | :--- | :--- |
| 3 | 96.868 | 63.288 |
| 4 | 92.644 | 65.532 |
| 5 | 80.907 | 63.400 |
| 6 | 79.335 | 63.070 |
| 7 | 73.009 | 62.402 |
| 8 | 65.177 | 62.782 |
| 9 | 62.512 | 62.551 |
| 10 | 63.044 | 61.760 |
| 11 | 61.836 | 61.140 |
| 12 | 60.704 | 60.820 |
| 13 | 57.946 | 61.468 |
| 14 | 57.388 | 61.629 |
| 15 | 57.371 | 61.424 |

Table 4- Global polynomial results for flat area

| Polynomial type | RM SE of check points (m) | RM SE of control points (m) |
| :--- | :--- | :--- |
| Linear poly. | 71.556 | 60.673 |
| Bilinear ploy. | 67.853 | 36.782 |
| Quadratic ( type 1) | 57.928 | 21.92 |
| Quadratic ( type 2) | 73.486 | 17.598 |
| Quadratic ( type 3) | 55.676 | 18.642 |
| Quadratic ( type 4) | 58.636 | 15.738 |

Table 5- Global polynomial results for mountainous area

| Polynomial type | RM SE of check points (m) | RM SE of control points (m) |
| :--- | :--- | :--- |
| Linear poly. | 107.447 | 76.651 |
| Bilinear ploy. | 122.229 | 40.377 |
| Quadratic ( type 1) | 97.196 | 34.971 |
| Quadratic ( type 2) | 108.518 | 29.344 |

Table 6-2D projective transformation result

| M ethod | RM SE of check points (m) | RM SE of control points (m) |
| :--- | :--- | :--- |
| 2D projective trans. | 348.9126 | 412.698 |

Table 7- RM SE of check points obtained by DLT (method 1)

| M ethod | X \& Y RM SE of check points (m) | Z RM SE of check points (m) |
| :--- | :--- | :--- |
| DLT | 124.513 | 413.665 |



Fig. 5- Control and check points in blue and red, respectively.


Fig. 6- Distributions of check and control points: green points are control ones located in flat area, blue points are represented the check points in mountainous area while the red ones illustrate the check points located in flat areas

Table 1- Information of SAR images used here

| Information | Des. Image 1 | Des. Image 2 | A sC. Image |
| :--- | :--- | :--- | :--- |
| Product type | SLC | SLC | SLC |
| Sensor mode | Image | Image | Image |
| Source | ASAR | ASAR | ASAR |
| Acquisition date | $2003 / 06 / 11$ | $2003 / 12 / 23$ | $2004 / 01 / 25$ |
| Product ID | ASA_IM S_IP | ASA_IM S_1P | ASA_IM S_1P |
| Orbit number | 6687 | 9192 | 9958 |
| Satellite ID | N1 | N1 | N1 |
| Range Sample spacing in meters | 7.80397463 | 7.80397463 | 7.80397463 |
| Azimuth sample spacing in meters | 4.050520072 | 4.050520072 | 4.050520072 |
| Azimuth sample spacing in time | $0.000605(\mathrm{~s})$ | $0.000605(\mathrm{~s})$ | $0.000605(\mathrm{~s})$ |
| Incidence angle in Near range | 18.596622 | 18.572363 | 18.560648 |
| Incidence angle in Far range | 26.147577 | 26.142576 | 26.145206 |
| Number of range lines | 26888 | 26897 | 23588 |
| Number of samples per range line | 5167 | 5167 | 5170 |

Table 2- Results of different polynomials.

| Polynomial type | RM SE of check points (m) | R M SE of control points (m) |
| :--- | :--- | :--- |
| Linear poly. | 82.249 | 82.769 |
| Bilinear ploy. | 80.203 | 78.659 |
| Quadratic ( type 1) | 59.357 | 57.808 |
| Quadratic ( type 2) | 66.342 | 35.545 |
| Quadratic ( type 3) | 57.370 | 56.307 |
| Quadratic ( type 4) | 58.501 | 55.790 |



Fig. 1- (a) ETM +image and (b) shaded relief of the study area.


Fig. 2- Distribution of check and control points of 6687 SAR image in red and green, respectively.


Fig. 3- Control and check points of images 6687 and 9192 in blue, green and red, respectively.


Fig. 4- Common control and check points of images 6687 and 9192 in blue and red, respectively.

$$
\begin{align*}
& \left(X-X_{S}\right)^{2}+\left(Y-Y_{S}\right)^{2}+\left(Y-Y_{S}\right)^{2}=R^{2}  \tag{10}\\
& \left(\dot{X}-\dot{X}_{S}\right)\left(X-X_{S}\right)+\left(\dot{Y}-\dot{Y}_{S}\right)\left(Y-Y_{S}\right)+\left(\dot{Z}-\dot{Z}_{S}\right)\left(Z-Z_{S}\right)=\frac{\lambda R f_{D}}{2}
\end{align*}
$$

where ( $X, Y, Z$ ) is the unknown geographic position of the target point to be solved, $(X, Y, Z)$ is the sensor position at the time of point acquisiti on, ( $\left.\dot{X}_{s}, \dot{Y}_{s}, \dot{Z}_{s}\right)$ is the velocity vector of the target point and ( $\left.\dot{X}_{s}, \dot{Y}_{s}, \dot{Z}_{s}\right)$ is the sensor velocity vector which can be determined by the attitude angles and moving speed of the sensor along the orbit. There are three unknown parameters $(X, Y, Z)$ and two equations that are not sufficient to estimate the unknown parameters. Therefore a stereo pair of image should be used. However, in the ephemeris data available in this study, there was no information about the Doppler centroid. Hence, we were not able to establish the Doppler equation. In order to compute the unknown coordinates, instead of two images, three SAR images had to be used: two descending images and one ascending one.
In order to estimate the unknown SAR model parameters, totally 10 check and control points were captured in three images. 4 points were used as control points while 6 points were exploited as check points as shown in Figure 5.

It was found that to mix the points of different areas (flat and mountainous) results in inaccurate processing parameters. Therefore, the control points were selected in the flat area. Among the check points two are located in the flat area in the vicinity of the control points while the others are placed in the mountainous area.
The differences between the computed control and check points coordinates and their real values are given in Table 11.

In Figure 6, the control points are in green, check points in blue and those check points which are located in the flat area are depicted in red.

Considering the poor distribution of the GCPs, it is obvious that the model is not fitted appropriately to the mountainous area. Due to the lack of GCPs in the study area, it was not possible to fit a better model to the mountainous area.

## 5. Conclusions and Discussion

Applying the 2D math models, it was possible to correct SAR images without considering the imaging geometry. The results showed that the main part of the error existing in SAR images can be modeled through 2D polynomials. Since the

SAR images used in this study are in slant range geometry, it was expected that considering the imaging geometry might lead us to the better results. In 3D geometric correction, the proposed SAR rigorous model exploited the available topographic data to calibrate the satellite ephemeris data. Using the refined SAR processing parameters, we were able to geocode the SAR imagery with an assumption that the used GCPs are error-free. The calibration was done by an iterative LS method applying the ephemeris data as initial values. As it was found, this method is very sensitive to the GCPs type. Since the points located in the flat areas were used for parameters refinement, the model was fitted to the flat area. However, in comparison with other methods, the results achieved by the rigorous SAR model were not accurate enough. The reasons would be:

1. The first and foremost reason is that the base to height ratio of the employed images was so small that the satellite configuration is poor. In order to obtain the required accuracy in DEM extraction, the baseline must be larger than 250 m . The more the baseline is, the more the accuracy of the extracted DEM is. However, in this study the baseline is less than 50 m . Because the available data was provided for the interferometry purpose.
2. Due to the lack of distinguishable features in the images and low radiometric quality of them, it was not possible to capture adequate control points.
3. Collecting of control points was a difficult task regarding inherent SAR error such as foreshortening and layover.
4. The available control points are not distributed uniformly in the study area.
5. The proposed rigorous SAR model is sensitive to the area type. If a model is fitted to the flat area, it can not be suitable for hilly or mountainous areas.
6. The last but not least is that the ephemeris data did not include any information about Doppler centroid. Therefore, we had to use one extra image (an ascending one) to make sufficient equations. To combine three images in order to extract the ground coordinates caused the image errors added together and made the results inaccurate
As a final conclusion, in order to obtain more accurate results in rigorous SAR model, the images should be appropriate regarding the geometry and accessibleephemeris data. In case of lacking such proper information, using 2D polynomials would be recommended.
algorithms the homologous points are extracted (matching) and the operator plays the role of supervisor. In this study, the first approach was exploited. The entire Radargrammetry procedure consists of two main steps:

1- The accurate geometric correspondence between image and object space must be established refining SAR images parameters.
2- A n inverse trisection problem must be solved to obtain the coordinates of each terrain points. The image coordinates of those points are found through a correlation process.

In order to establish the image to object correspondence, a rigorous SAR Image Formation Model (SIFM) must be defined. In this approach the model parameters whose accuracies are inadequate have to be refined based on calibration using control points.

### 4.2.2.1. SAR Image Formation Model (SIFM)

The model used here is based on two basic SAR mapping equations called range and Doppler equations as follows (Liu et. al., 2004):
$R(t)=\sqrt{(\vec{S}(t)-\vec{P}(t)) \cdot(\vec{S}(t)-\vec{P}(t))}=|\vec{S}-\vec{P}|=S P$
$f_{D}=-\frac{2 \cdot \overrightarrow{S P} \cdot \vec{V}_{S}}{\lambda \cdot S P}$
where $\vec{P}(t)=(X, Y, Z)$ and $\vec{S}(t)=\left(X_{S}, Y_{S}, Z_{S}\right)$ are the locations of the target point on the ground and the satellite, respectively. It should be noticed that these coordinates are stated in the earth-fixed coordinates system (CT). $\vec{V}_{S}(t)=\left(\dot{X}_{S}, \dot{Y}_{S}, \dot{Z}_{S}\right)$ is the satellite velocity vector, $R(t)$ is the slant range distance, $f_{D}$ is the Doppler centroid frequency and $\lambda$ is the radar wavelength. The SIFM includes different groups of parameters: orbital parameters, sensor parameters and SAR processing parameters.
Using at least three sets of satellite position vectors available in the satellite ephemeris data, the sensor position can be modeled by:
$X_{s}=a_{0}+a_{1} t+a_{2} t^{2}+a_{3} t^{3}$
$Y_{S}=b_{0}+b_{1} t+b_{2} t^{2}+b_{3} t^{3}$
$Z_{s}=c_{0}+c_{1} t+c_{2} t^{2}+c_{3} t^{3}$
where $a_{i}, b_{i}, c_{i} \quad(i=0,1,2,3)$ are fitted coefficients. The Doppler centroid varies along azimuth and range direction and can be approximated applying the satellite ephemeris data as follows:
$f_{D}=d_{0}+d_{1} R+d_{2} R^{2}+d_{3} t+d_{4} t^{2}$
where $d_{i} \quad(i=0,1,2,3)$ are fitted coefficients, R is the slant range and $t$ is the time. For a given target the acquisition time $t$ is related to the azimuth coordinate (lin) of the SAR image by:
$t=t_{0}+\Delta t .(l i n-1)$
where $\Delta t$ is the azimuth sample spacing in time which is related to the pixel spacing in azimuth direction and $t_{0}$ is the time acquisition of the first image line.
The slant range is related to the slant range coordinate (col) as follows:
$R_{S}=R_{S 0}+\Delta R .(\operatorname{col}-1)$
where $R_{S 0}$ is the near slant range and $\Delta R$ is the pixel size in range. Some of the model parameters are known with inadequate accuracy. In order to obtain an accurate geolocation, these parameters must be refined by a Least Square calibration using GCPs. In this method we have to use a stereo pair of SAR images. The unknown parameters are: the near slant range $R_{S 0}$, the acquisition time of the first image line $t_{0}$, the pixel size in range and azimuth direction $\Delta R$ and $\Delta \mathrm{t}$,respectively and the coefficients of the orbit polynomials. These parameters are considered constant in a SAR image scene. In order to obtain geometric consistency, the joint calibration was used to estimate the unknown parameters of two images simultaneously (block adjustment). The adjustment is carried out with a LS iterative procedure and the unknown parameters are estimated in a very good convergence. The total gradient in the convergence problem reached to 0.0000001 after 130 iterations.

### 4.2.2.2. Derivation of 3D coordinates of homologous points by space resection

With the image coordinates $\left(\operatorname{lin}_{i}, \operatorname{col}_{i}\right)$, of the target point, two SAR equations can be formed (Crosetto, et. al. ). By rewriting the range and Doppler equations we obtain:

### 4.2. 3D Geometric correction

There are different approaches in order to do 3D geometric correction of the image. These models is mostly used in order to orthorectify the satellite images (relief displacement reduction) or to generate the DEM . For DEM generation after 3D math model definition, a stereo pair of images is needed. While working with SAR data, two images acquired from different positions in the space are exploited. The distance betw een two acquisition stations is called baseline. The larger the baseline is, the more accurate the extracted DEM is. In the following sections several techniques are introduced and tested on SAR data.

### 4.2.1. Direct Linear Transformation (DLT)

The first step in using this method is to define the appropriate model for two descending images (6687 and 9192) and the second one is to exploit two images in order to compute the height corresponding to each point. DLT transformation is a special case of 3D projective transformation defined as follows:

$$
\begin{align*}
& x=\frac{L_{1} X+L_{2} Y+L_{3} z+L_{4}}{L_{9} X+L_{10} Y+L_{11} z+1}  \tag{4}\\
& y=\frac{L_{5} X+L_{6} Y+L_{7} z+L_{8}}{L_{9} X+L_{10} Y+L_{11} z+1}
\end{align*}
$$

This method has been used in to different ways:

1. Coefficients estimation of each image separately: employing 16 and 13 GCPs for images 6687 and 9192, respectively, DLT coefficients for each image were estimated separately. In order to test the results, 8 common check points of both images (homologous points) were selected and the ground coordinates including $X, Y$ and $Z$ were calculated. The results are given in Table 7.

The differences between the computed and original coordinates of check points are given in Table 8.
AS it can be observed, the accuracy of $X, Y$ and specially $Z$ is very low. The reasons may be:
-The baseline is very small due to the SAR images used. N ormally it must be more than 250 m for obtaining required precision in height estimation. However the baseline is less than a couple of 10 meters. Therefore, the satellite configuration does not have the required consistency. This fact affects the accuracy of the results.
-The quality of GCPs is relatively low.
-The last but not least is that the control and check points do not have the satisfying distributions due to the lack of homologous points.

In Figure 3, the control points of images 6687 and 9192 are shown in blue and green while the check points are illustrated in red.
For more geometric consistency, the images should be modeled together using the same control points. Therefore, it is preferred to apply the second method.
2. Using homologous points of these two images and coefficients estimation of both images together: in this method two images are modeled simultaneously using 7 GCPs and 2 check points. The results are shown in table 9. The differences between the computed and original coordinates of check points are depicted in table 10.
It should be noted that there is one check point common in evaluating both methods which is highlighted in Tables 8 and 10. A Ithough the number of used GCPsin the second approach is much less than the first one, the results are more reliable. Figure 4 illustrates the distribution of GCPs and check points. The better results in 3D geometric correction can be obtained while considering the imaging geometry at the time of imaging. Since the SAR imaging is different from other types of sensors, a specific model is needed for SAR geometric correction. In the following section a rigorous geometric SAR model will be presented.

### 4.2.2. Radargrammetry - a Rigorous Geometric SAR Model

By the advent of SAR data, new algorithms have been developed to generate DEM. Starting from SAR images, DEM can be produced using either the amplitude (radargrammetry or shape from shading techniques) or phase (interferometry). R adargrammetry is the technology of extracting geometric object information from radar images (Leberl, 1990). Radargrammetry uses amplitude SAR images applying the same approach that photogrammetry uses with optical images. This technique is employed with stereoscopic pairs acquired from the same side but with different incidence angles. Radargrammetry can be implemented using an interactive approach or an automatic one. In the former method, the operator must capture the data manually while in the latter based on image correlation
points of the first descending image (6687) used in 2D geometric correction.

### 4.1.1. Interpolative Models

This method corrects the images geometrically without considering the imaging geometry at the time of imaging. A math model which is mostly a polynomial is applied to relate the image and ground space.
Using the first data set of 6687 descending SAR image, the best polynomial fitted to the area was selected according to the check points RMSE (Root M ean Square Error) using different interpolative methods. It should be noticed that before geometric correction the image was downsampled to the resolution of 20 meters. A mong 24 points selected from the topographic map, 15 points were used as control points and the rest of them were considered as check points. The 2D math models tested on the image are as follows:

1. Global polynomial: In this method one general $2 D$ polynomial is fitted to the whole image. As mentioned before the best polynomial is selected based on the RMSE of the check points. Several polynomials were tested including Linear, Bilinear and different forms of quadratic one. The results are depicted in Table 2.

As it can be seen, the best polynomial fitted to the image is quadratic type 3 defined as follows:

## Quadratic type 3:

$X=a_{0}+a_{1} x+a_{2} y+a_{3} x y+a_{4} x^{2}+a_{5} x^{2} y$
$Y=b_{0}+b_{1} x+b 2 y+b_{3} x y+b_{4} x^{2}$
2. Point wise: In this model after selection of the best global polynomial, the computed coordinates of each unknown point will be corrected based on a couple of effective control points selected based on different strategies. The simplest strategy to select the effective control points is based on their nearness to the unknown point. This method was tested using different number of effective control points. In order to refine the calculated coordinates, based on the effective control points, two different methods called moving average and weighted distance were applied. A s a result the residual vectors should be reduced in each unknown point. Table 3 shows the results of point wise method applying different number of effective points which are the nearest ones.

As it is shown in Table 3, the point wise results are not satisfying as it was expected before. The reason is that the effective control points selection strategy which was based on the distance is not proper enough in this image because the image is a mixture of various types of area. It is mostly preferred to take a supervised method to select the effective control points.
3. Piece wise: Since the image is a mixture of several regions with different topographic characteristics, a unique polynomial can not be fitted very well to the whole image. Therefore, the most proper thing to do is to split the image into different regions and fit a specific polynomial to each part of the image. The image 6687 is a combination of hilly and flat areas. Hence, different polynomials were tested to each area separately. The results are given in Tables 4 and 5. According to these tables, the best polynomials fitted to the flat and mountainous areas are quadratic type 3 and 1, respectively as shown in Eqs. (1) and (2).

$$
\text { Quadratic type 1: } \quad \begin{array}{ll} 
& X=a_{0}+a_{1} x+a_{2} y+a_{3} x^{2}  \tag{2}\\
& Y=b_{0}+b_{1} x+b 2 y+b_{3} x^{2}
\end{array}
$$

4. 2D projective transformation: The mathematical model used here is as follows:
$x=\frac{L_{1} X+L_{2} Y+L_{3}}{L_{7} X+L_{8} Y+1}$
$y=\frac{L_{4} X+L_{5} Y+L_{6}}{L_{7} X+L_{8} Y+1}$

This method assumes that the height difference in the area is zero. However, our study area does not have such a characteristic. Therefore, it is expected not to get satisfying results using this algorithm.
The results shown in Table 6 prove our claim.

### 4.1.2. Parametric models

This model considers the imaging geometry. Each error source is recognized and modeled in this method. Then the imaging geometry is corrected regarding the modeled errors. Since, the recognition and modeling of all errors is impossible, this method is rarely used. In our study this method is ignored due to the mentioned reason.


## 1. Introduction

A SAR (Synthetic A perture Radar) is a distance-measuring device. The RADAR system measures the time delay between transmission and reception of a pulse in order to determine the target's location with respect to another one in the range direction. This kind of data recording causes spatial distortions in SAR data. W hen a satellite SAR is imaging a steep relief feature such as a mountain, the RADAR pulse could reach the top of the mountain first and the bottom of the mountain last. Therefore, from the SAR's perspective, the top of the mountain is closer than the base of the mountain. As a result the mountain appears to be leaning toward the sensor, causing the displacement of mountain tops and other topographic features from their orthographic positions. These distortions make SAR data completely different from other remotely sensed data type, and consequently the SAR sensor model differs form optical sensor models. In this paper, in order to model the spatial distortions in the SAR images, different approaches were applied. In the next section the study area and the data used are introduced. Section 2 presents the preprocessing steps which are essential to preparing data. Section 3 is devoted to geometric correction including 2D and 3D math models. Some concluding remarks are given in the last section.

## 2. Study area and available SAR data

In this study, different math models were tested with ENVISAT A SA R (A dvanced Synthetic A perture Radar) data of $B$ am area. There are differentA SA R products available for different applications. The product used here is Image M ode Single-L ook Complex (A SA _IM S_1P). Image M ode SingleLook Complex is phase-preserved image generated using up-to-date auxiliary parameters. A uxiliary data is essential to processing which is used to produce a product. These data may include calibration data measured on-board but is not part of the main measurement data of the instrument. It may also include external calibration files from sources other than the satellite, processor configuration files, and any other files needed by instrument processor. Generally, these types of product are called SLC. These data cannot be used directly unless a couple of pre-processing procedures have been done on them. In order to prepare SA R data, B asic ENVISAT SA R Toolbox (BEST) was applied. This software is a widely used package for ENVISAT data pre-processing and preparing them for further processing.

There were 3 SLC images available for BAM area. Two of them were acquired in descending mode, while the third one's acquisition mode is ascending. Two descending images nearly cover the same area since the baseline is a couple of ten meters which is small. However, since the acquisition geometry of the ascending mode is different, the overlapped area between them are very small. Bam city is located in a relatively flat area. In north of Bam there is a mountainous area which is subject to foreshortening, layover and shadow. Figure 1 illustrates the ETM + image and shaded relief of the study area extracted from SRTM DEM .

## 3. Pre-processing SAR data

As mentioned before BEST software was applied for preparing SAR data. In this step after full resolution SAR image extraction using header information, the complex image is converted in to amplitude.
Since SAR is a coherent imaging system, the image is subject to speckle noise, which reduces the image quality. In order to reduce the speckle noise an adaptive filter called Lee with the window size of 3 was used.
Table 1 shows the SAR images information used in this study.
A fter pre-processing step, different math models including 2D and 3D models are applied on the images and the results are compared together.

## 4. Geometric correction

The first and foremost step in geometric correction is Ground Control Points (GCPs) collection. The most suitable GCPs sources available here is digital topographic map of the area with the scale of $1: 25,000$. The projection system is UTM and the area is located in zone 40. The reference ellipsoid is WGS84. For 3D math models, elevation information was extracted using SRTM DEM with the resolution of 80 m . Although the used DEM is very course compared to SAR data, the height accuracy is quite acceptable. In this section numerous mathematical models will be tested on SAR images.

### 4.1. 2D geometric correction

The images are corrected with respect to the $x$ and $y$ coordinates using 2D geometric correction models. There are two general types of 2D math models which are explained in the following sections.
Figure 2 shows the distribution of the control and check

# برر سى مدلهاى رياضى دو بعدى و سه بعدى براى تصحيح هندسى تصاويررادارى SAR (مطالعه موردى در منطقه بم) 

نوشته: مريم دهقانى**، محمد جواد ولدان زوج ج على منى منصوريان


# Study of 2D and 3D Geometric Models Applied on SAR Images (A case study in BAM area) 

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برخورداراست.
كليد وارْهها: رادار، تصاوير SA R، تصحيح هندسى، نقطه كترل، رادار گرامترى


#### Abstract

study several 2D and 3D math models have been tested in order to correct slant range SAR data geometrically. Some of these models consider the imaging geometry at the time of imaging while the others relate the ground space to the image one by mathematical polynomials. The images used here are 3 ENV ISAT ones of Bam area. In order to extract the 3D GCPS, a topographic map with a scale of 1:25000 and SRTM DEM were used. The 2D math models used in this study include Global polynomial, Point wise, Piece wise and Projective while the 3D models are DLT and Rigorous SA R model. Since the images used in this study were originally ordered for interferometry studies, their baseline is so small that the precision of 3D coordinates extraction is not satisfactory enough. However, the results of 2D models are much better.


Key words: RA DA R, SAR images, Geometric correction, Control point, R adargrammetry

ا- مقاله ارائه شده در ارتباط با زمينشناسى و علوم زمين باشد.
 r- مقاله در نرم افزار W ord نسخه 2003 يا XP تايب شود.
 و فاصله سطرها ا/ ا/ برابر در نظر گرفته شود. تمامى متن مقاله نيز در يكك ستون تنظيم گردد.
 براى متن قلم زر זّا در نظر گرفته شود. اندازه فونت انگا
 نوشته مى شود.
Vزيرنويس صفحات خود دارى شود). - - در تمام متن "ها" جمع پيوسته، "تر "و "ترين " جدا نوشته شود.

 شوند.

- ا- الگُوى مرجع نويسى در بخش كتابنگارى با توجه به نمونههاى زير و رعايت حروف بزر گَ و ايتاليك نوشته شود:
-     - ا- مقالات:

سهيلى، م.، اوצ|- شرح نقشه زمين شناسى نيمه جنوبى جهار گوش كوه كورخود، سازمان زمين شناسى كشور، • • الصفحه
B atchelor, R.A. \& B owden P. , 1985- Petrogentic interpretation of granitoid rock series using multicationic parameters, chemical geology, 48: 43-55.
-
W etzel R.G., 1983- Limnology, $2^{\text {nd }}$ edition. Saunders publishing company, 582 p.

Smith A.C.S. \& M udder T.I., 1999- The environmental geochemistry of eyanide. in : Plumlee G.S., \& Logsdon M .J. (eds.) The Environmental Geochemistry of M ineral Deposits. Society of Economic Geologists. PP2q-z48

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\begin{aligned}
& \text { 11- كلمهها و متون داخل جدولها و شكلها تا حد امكان فارسى شود. } \\
& \text { rir }
\end{aligned}
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 الكترونيكى باشد.

 مقاله نياز به اصلاحيه داشته باشد، مقاله اصلاح شده در دو نسخه (يكك نسخه با ذكر مشخصات كامل نويسنده و يكك نسخه بـدون مشخـصات نويسنده) بــه دفتر فـصلنامه ارسـال گردد. در صورت وجود هر گونه نقص در مدار كك، مقاله عودت داده مىشود.



 زيرنويس شكلها و زير نويس جلدولها به صورت JPG خوددارى گردد. موارد ذكر شده بايستى در W ord تنظيم شده باشند.
 CD حاوى فايل كامل مقاله (به صورتى كه ذكرشد)، لازم بوده و بايستى پس از اخذ نامهٔ پذ يرش، و اعمال كلئَاصلاحات پيشنهادى داوران، صورت گيرد.

 براى داورى مقاله توسط داوران معرفى شده و جود ندارد.

